

Tables Useful for the Calculation of the Molecular Integrals XIV

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The Integrals of type $\int \alpha_a^*(1)f(\mathbf{r})\beta_b(1)dv$, where $f(\mathbf{r})=x \pm iy, z, x^2+y^2$ and z^2 were calculated by using IBM 650. A part of the results was already published as Table XL, XLI, XLII and XLIII in Part XII¹⁾ and XIII²⁾ of this series. Some of the remaining results will be given in this paper. These integrals can be expressed in terms of the parameters $A=\alpha_n=\delta_n R$ and $B=\alpha'_n=\delta'_n R$, where δ_n and δ'_n are the orbital exponents for the two atoms A and B respectively and R is the inter-nuclear distance. The numerical tables are as follows.

Table XLIV.

$$XX+YY, 12=1/R^2 \cdot \int (1s)_a(x^2+y^2)(2s)_b dv,$$

$$XX+YY, 13=1/R^2 \cdot \int (1s)_a(x^2+y^2)(2p\sigma)_b dv,$$

$$ZZ, 12 = 1/R^2 \cdot \int (1s)_a z^2 (2s)_b dv,$$

$$ZZ, 13 = 1/R^2 \cdot \int (1s)_a z^2 (2p\sigma)_b dv,$$

for $A=10.00$ (0.25) 25.00 and $B=1.00$ (0.25) 10.00. In giving the numerical values, the floating digit is taken as explained in Part XII. The integrations are performed by using the following formulae.

$$\begin{aligned} 17) \quad XX+YY, 12 &= \frac{1}{32\sqrt{3}} \sqrt{\alpha_1^3 \alpha_2'^5} \{ A_5(B_0-B_2) - A_4(B_1-B_3) \\ &\quad - A_3(B_0-B_4) + A_2(B_1-B_5) + A_1(B_2-B_4) - A_0(B_3-B_5) \}, \end{aligned}$$

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$$\begin{aligned}
18) \quad XX + YY, 13 &= \frac{1}{32} \sqrt{\alpha_1^3 \alpha_2'^5} \{A_5(B_1 - B_3) - A_4(B_0 - B_2) \\
&\quad - A_3(B_1 - B_5) + A_2(B_0 - B_4) + A_1(B_3 - B_5) - A_0(B_2 - B_4)\}, \\
19) \quad ZZ, 12 &= \frac{1}{32\sqrt{3}} \sqrt{\alpha_1^3 \alpha_2'^5} (A_2 B_5 - A_3 B_4 - A_4 B_3 + A_5 B_2), \\
20) \quad ZZ, 13 &= \frac{1}{32} \sqrt{\alpha_1^3 \alpha_2'^5} (A_2 B_4 - A_3 B_5 - A_4 B_2 + A_5 B_3),
\end{aligned}$$

where $\alpha_1 = \delta_1 R$, $\alpha_2' = \delta_2' R$, $A_n = A_n \left(\frac{\alpha_1 + \alpha_2'}{2} \right)$ and $B_n = B_n \left(\frac{\alpha_1 - \alpha_2'}{2} \right)$. A_n and B_n are the auxiliary functions explained in Part XII.

Errata to Part XII and XIII

	Page	Line	
Part XII	31	heading	Natural Science Report, Ochanomizu University, Vol. 13 , No. 2, 1962.
	32	heading	NSR., O. U., Vol. 13 .
	16	5)	$Z, 13 = \frac{1}{16} \sqrt{\alpha_1^3 \alpha_2'^5} (A_4 B_2 - \dots)$
	17		$\alpha_2' = \delta_2' R$
Part XIII	37	footnote	NSR. O. U., 13 , 31 (1962)
	70	1	Table XLIII.

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References

- 1) Natural Science Report, Ochanomizu University, **13**, 31 (1962).
- 2) Natural Science Report, Ochanomizu University, **14**, 37 (1963).